

Solutions

HW #10

ECE - 606, Fall 2012

Q1

$$W = \sqrt{\frac{2\epsilon_s \phi_s}{q N_A}}$$

Substituting known values

$$\phi_s = \frac{q N_A W^2}{2\epsilon_s} = \underline{0.1914 \text{ V}}$$

62
16.12

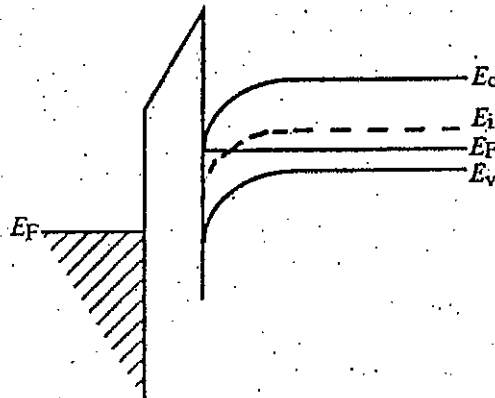
(a) Curves *a* and *b* are standard low- and high-frequency *C-V* curves that result when the semiconductor component of the MOS-C is in equilibrium under d.c. biasing conditions. Curve *c* is a nonequilibrium deep-depletion characteristic.

(b) In accumulation $C \rightarrow C_0 = K_0 \epsilon_0 A_G / x_0$. Since both devices exhibit the same capacitance in accumulation, the two devices have the same oxide thickness. With x_0 being the same, the lower capacitance of device *b* in inversion indicates this device has a lower doping. (W_T increases with decreasing doping, thereby giving rise to a smaller capacitance; also see Fig. 16.14b.)

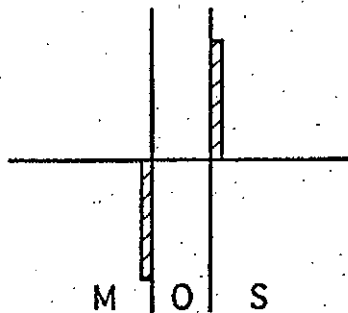
63
16.13

(a) *p*-type ... For *p*-type devices accumulation (C_{max}) occurs for negative V_G and inversion (C_{min}) occurs at positive V_G . The exact opposite is true for *n*-type devices.

(b) At point (2) the *p*-type MOS-C is far into inversion. Thus



(c) At point (1) the MOS-C is clearly deep into accumulation.



(d) From Fig. P16.13, $C_{\max} = 100\text{pF}$. However,

$$C_{\max} = C_0 = \frac{K_0 \epsilon_0 A G}{x_0}$$

$$x_0 = \frac{K_0 \epsilon_0 A G}{C_{\max}} = \frac{(3.9)(8.85 \times 10^{-14})(3 \times 10^{-3})}{(10^{-10})} = 0.104 \mu\text{m}$$

(e) In the delta-depletion formulation

$$C = \frac{C_0}{1 + \frac{K_0 W_T}{K_S x_0}} \quad \text{inv } (\omega \rightarrow \infty) \quad (16.34d)$$

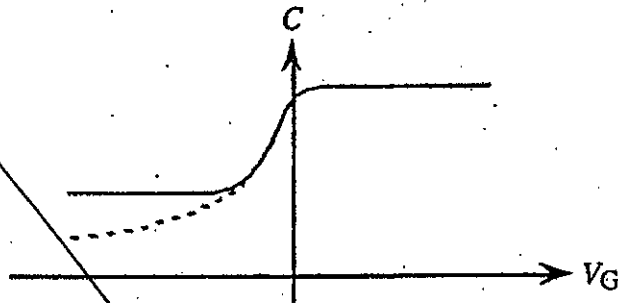
Thus

$$W_T = \frac{K_S x_0}{K_0} \left(\frac{C_0}{C} - 1 \right) = \frac{(11.8)(0.104)}{(3.9)} \left(\frac{100}{20} - 1 \right) = 1.26 \mu\text{m}$$

Employing Fig. 16.9, we conclude $N_A \cong 5 \times 10^{14}/\text{cm}^3$.

16.14

(a)



$$(b) C_{\max} = C_0 = \frac{K_0 \epsilon_0 A G}{x_0} = \frac{(3.9)(8.85 \times 10^{-14})(10^{-3})}{10^{-5}} = 34.5 \text{ pF}$$

$$(c) \phi_F = -(kT/q) \ln(N_D/n_i) = -0.0259 \ln(2 \times 10^{15}/10^{10}) = -0.316$$

$$W_T = \left[\frac{2K_S \epsilon_0}{qN_D} (-2\phi_F) \right]^{1/2} = \left[\frac{(2)(11.8)(8.85 \times 10^{-14})(2)(0.316)}{(1.6 \times 10^{-19})(2 \times 10^{15})} \right]^{1/2} = 6.42 \times 10^{-5} \text{ cm}$$

Q4 Short-channel MOSFET.

- 1) V_{th} reduction, the gate no longer controls the total gate depletion.
- 2) Mobility reduction.
- 3) High electric fields imply
 - a) Carrier velocity saturation
 - b) gate oxide charging
 - c) Impact ionization near the drain.
- 4) Punch-through
- 5) Channel length modulation.

Q5 $\phi_B = V_T \ln(N_A/n_i) = 0.35 \text{ V}$

$$\phi_s = \chi_s + \frac{E_g}{2q} + \phi_B = 4.95 \text{ V}$$

Q6 Hole concentration: $p = p_0 \exp(-\psi_s/V_T) = 2.1 \times 10^{14} \text{ cm}^{-3}$

Electron $n = \frac{n_i^2}{p_0} \exp(\psi_s/V_T) = \frac{1.6 \times 10^6}{10^6} \cdot 10^6 \text{ cm}^{-3}$

Q7 Max depletion: $W_{\max} = \sqrt{\frac{2\epsilon_s(2\phi_B)}{qN_A}} = 0.304 \mu\text{m}$

To compute V_{th}

(We have used $\phi_B = 0.35\text{V}$
from Q5)

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} = 3.45 \times 10^{-8} \text{ F/cm}^2$$

$$\psi_{ox} = \frac{qN_A W_{\max}}{C_{ox}} = 1.41\text{V}$$

$$V_{th} = \psi_{ox} + \psi_s = 1.41 + 0.7 = 2.11\text{V}$$

(Also $\psi_s = 2\phi_B$)

$$\therefore \psi_s = 0.7$$

— X —