

angle observation □: 0 0000 0 17-1

absolute encoder ▣: 1 0001 1

0010	2
0011	3
0100	4
⋮	
1111	15

$2^4 = 16$

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incremental encoder 17-2

A

B

B leads A  
90°

A ↓ ↑  
B L H  
+1 +1

A

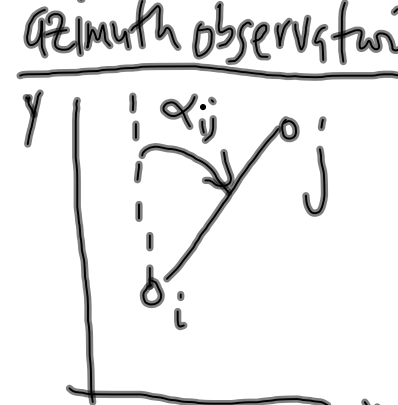
B

A leads B

A ↑ ↓  
B L H  
-1 -1

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azimuth observation



$$\alpha_{ij} = \tan^{-1} \left( \frac{x_j - x_i}{y_j - y_i} \right)$$

$$F_\alpha = \alpha_{ij} - \tan^{-1} \left( \frac{x_j - x_i}{y_j - y_i} \right) = 0$$

$$\frac{\partial F_\alpha}{\partial x_i} = -\frac{1}{1 + \left(\frac{\Delta x}{\Delta y}\right)^2} \cdot \frac{1}{\Delta y} (-1) = \frac{\Delta y}{\Delta x^2 + \Delta y^2} = \frac{\Delta y}{D_{ij}^2}$$

$$\frac{\partial F_\alpha}{\partial y_i} = -\frac{1}{1 + \left(\frac{\Delta x}{\Delta y}\right)^2} (-1) \frac{\Delta x}{\Delta y^2} (-1) = \frac{-\Delta x}{\Delta x^2 + \Delta y^2} = -\frac{\Delta x}{D_{ij}^2}$$

$$\frac{\partial F_\alpha}{\partial x_j} = \frac{-\Delta y}{\Delta x^2 + \Delta y^2}$$

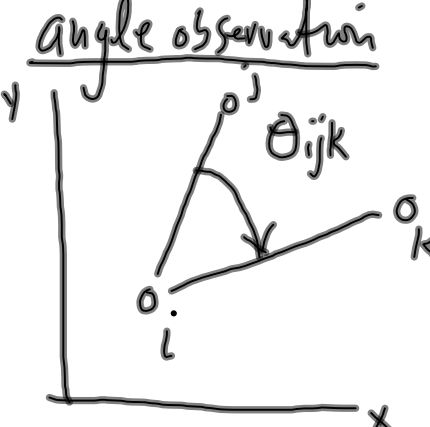
$$\frac{\partial F_\alpha}{\partial y_j} = \frac{+\Delta x}{\Delta x^2 + \Delta y^2}$$

~~17-3~~

$\Delta x = x_j - x_i$   
 $\Delta y = y_j - y_i$

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angle observation



$$\theta_{ijk} = \alpha_{ik} - \alpha_{ij}$$

$$\theta_{ijk} = \tan^{-1} \left( \frac{\Delta x_{ik}}{\Delta y_{ik}} \right) - \tan^{-1} \left( \frac{\Delta x_{ij}}{\Delta y_{ij}} \right)$$

$$F_\theta: \theta_{ijk} - \tan^{-1} \frac{\Delta x_{ik}}{\Delta y_{ik}} + \tan^{-1} \frac{\Delta x_{ij}}{\Delta y_{ij}}$$

$$\frac{\partial F_\theta}{\partial x_i} = -\frac{1}{1 + \left(\frac{\Delta x_{ik}}{\Delta y_{ik}}\right)^2} \cdot \frac{1}{\Delta y_{ik}} (-1) + \frac{1}{1 + \left(\frac{\Delta x_{ij}}{\Delta y_{ij}}\right)^2} \frac{1}{\Delta y_{ij}} (-1)$$

$$\frac{\Delta y_{ik}}{\Delta x_{ik}^2 + \Delta y_{ik}^2} - \frac{\Delta y_{ij}}{\Delta x_{ij}^2 + \Delta y_{ij}^2}$$

17.4

subscript should be ij

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$\frac{\partial F_0}{\partial x_j} = \frac{\Delta y_{ij}}{D_{ij}^2}$  ,  $\frac{\partial F_0}{\partial x_k} = -\frac{\Delta y_{ik}}{D_{ik}^2}$   $x_i, y_i, D_{ij}, D_{ik}$ : 17.5  
 evaluate at current value of approximation

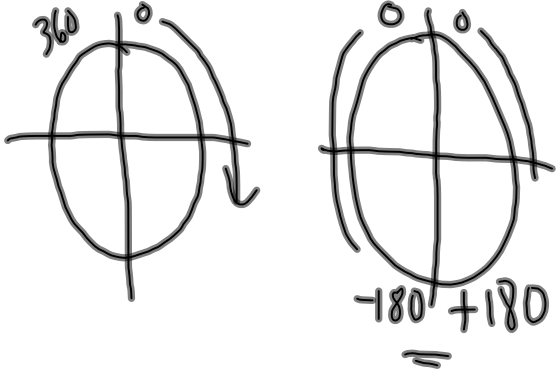
$\frac{\partial F_0}{\partial y_i} = -\frac{\Delta x_{ik}}{D_{ik}^2} + \frac{\Delta x_{ij}}{D_{ij}^2}$   $\Delta x_{ik} = x_k - x_i$   
 $\Delta x_{ij} = x_j - x_i$

$\frac{\partial F_0}{\partial y_j} = -\frac{\Delta x_{ij}}{D_{ij}^2}$

$\frac{\partial F_0}{\partial y_k} = \frac{\Delta x_{ik}}{D_{ik}^2}$

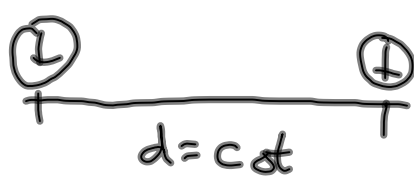
Right hand side vector  
 $f = -F(x, x^0)$

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be aware of discontinuity 17.6  
 $\epsilon_i$  fix by add or subtract  $2\pi$

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measuring distances:  
 steel tape  
 time of flight T.O.F.   
 $d = ct$

1 way ranging  
 clock synchronization

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2-way ringing

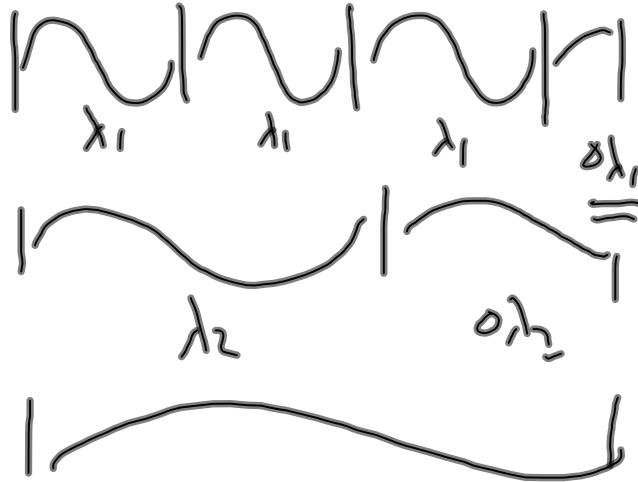


17-7

T.O.F.

$$d = \frac{1}{2} c \otimes t$$

Phase: more common terrestrial



$$D = m_1 \lambda_1 + \delta\lambda_1$$

$$D = m_2 \lambda_2 + \delta\lambda_2$$

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