

$$Q_{\Delta\Delta} = N^{-1}, \quad \hat{\underline{l}}, v, \quad \underline{\hat{l}} = \boxed{\quad} \cdot \underline{l}$$

$$y = Ax \quad 22-1$$

$$\Sigma_{yy} = A \Sigma_{xx} A^T$$

$$=$$

$$\hat{\underline{l}} = \underline{l} + v, \quad v + B\Delta = f, \quad v = f - B\Delta$$

$$\hat{\underline{l}} = \underline{l} + f - B\Delta, \quad f = d - \underline{l},$$

$$\hat{\underline{l}} = \underline{\underline{l}} + d - \underline{\underline{l}} - B\Delta, \quad \hat{\underline{l}} = d - B\Delta$$

$$\Delta = (B^T W B)^{-1} B^T W (d - \underline{l})$$

$$\hat{\underline{l}} = d - B (B^T W B)^{-1} B^T W (d - \underline{l})$$

$$\hat{\underline{l}} = \underline{\underline{d - B(B^T W B)^{-1} B^T W d}} + \underline{\underline{B(B^T W B)^{-1} B^T W \underline{l}}}$$

$$\begin{aligned}
 Q_{\hat{\beta}\hat{\beta}} &= \underbrace{B(B^T W B)^{-1} B^T W}_{N^{-1}} \cdot Q \cdot \underbrace{[B(B^T W B)^{-1} B^T W]^T}_{W B (B^T W B)^{-1} B^T} \\
 &= \underbrace{B(B^T W B)^{-1} B^T W}_{N^{-1}} \cdot \boxed{Q \cdot W} \cdot \underbrace{B(B^T W B)^{-1} B^T}_{W B (B^T W B)^{-1} B^T}
 \end{aligned}$$

$$\boxed{Q_{\hat{\beta}\hat{\beta}} = B N^{-1} B^T} \quad \Sigma_{\hat{\beta}\hat{\beta}} = \sigma_0^2 Q_{\hat{\beta}\hat{\beta}}$$

$$Q_{vv} = ? \quad \underline{v = \square \cdot \underline{\beta} + \text{const.}}$$

$$Q_{vv} = \square Q_{\beta\beta} \square^T$$

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$$V = f - B\Delta, \quad v = d - l - B N^{-1} B^T W (d - l)$$

$$v = d - l - B N^{-1} B^T W d + B N^{-1} B^T W l$$

$$v = \underbrace{(I - B N^{-1} B^T W)}_{\text{constant vector}} d + \underbrace{(B N^{-1} B^T W - I)}_{\square} l$$

$$Q: Q_{ll}$$

$$\begin{aligned} Q_w &= (B N^{-1} B^T W - I) Q (B N^{-1} B^T W - I)^T \\ &= (B N^{-1} B^T - Q) (W B N^{-1} B^T - I) \end{aligned}$$

$$(BN^{-1}B^T - Q)(WBN^{-1}B^T - I)$$

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$$\underbrace{BN^{-1}B^T WBN^{-1}B^T}_{BN^{-1}B^T} + Q - BN^{-1}B^T - BN^{-1}B^T$$

$$BN^{-1}B^T + Q - BN^{-1}B^T - BN^{-1}B^T$$