

Relationship between  $\chi^2$  &  $F$

24-1

$$X \sim F_{r, \infty} \Rightarrow r \cdot X \sim \chi^2_r$$

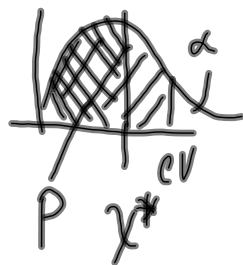
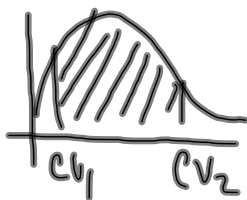
conversely

$$X \sim \chi^2_r \Rightarrow \frac{X}{r} \sim F_{r, \infty} \leftarrow$$

$$\chi^* = \frac{V^T W V}{\sigma_0^2} \sim \chi^2_r \quad \text{--- Chi-squared test}$$

$$\frac{\frac{V^T W V}{\sigma_0^2}}{r} \sim F_{r, \infty} \quad \frac{\frac{V^T W V}{r}}{\sigma_0^2} = \frac{\hat{\sigma}_0^2}{\sigma_0^2} \sim F_{r, \infty} \quad \text{--- F test}$$

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$$A = 1 - P$$

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reject  $H_0$  if  $A < \alpha$   
accept otherwise

$$\chi^*, \quad P = \text{cdf}(\text{'chi2'}, \chi^*, r)$$

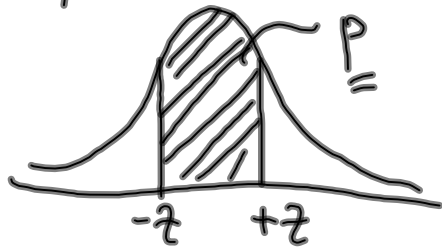
consequences of not passing global test

$$\sigma_0^2 \cdot X \quad \left\{ \begin{array}{l} \Sigma_{xx} = \sigma_0^2 Q_{xx} \quad (\text{crossed out}) \\ \Sigma_{xx} = \hat{\sigma}_0^2 Q_{xx} \end{array} \right. \quad \hat{\sigma}_0^2 = \frac{V^T W V}{r}$$

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Confidence interval for 1 RV

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$$\text{Prob}(-z < R < +z) = F(z) - \underline{F(-z)}$$

$$F(-z) = 1 - F(z)$$

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