

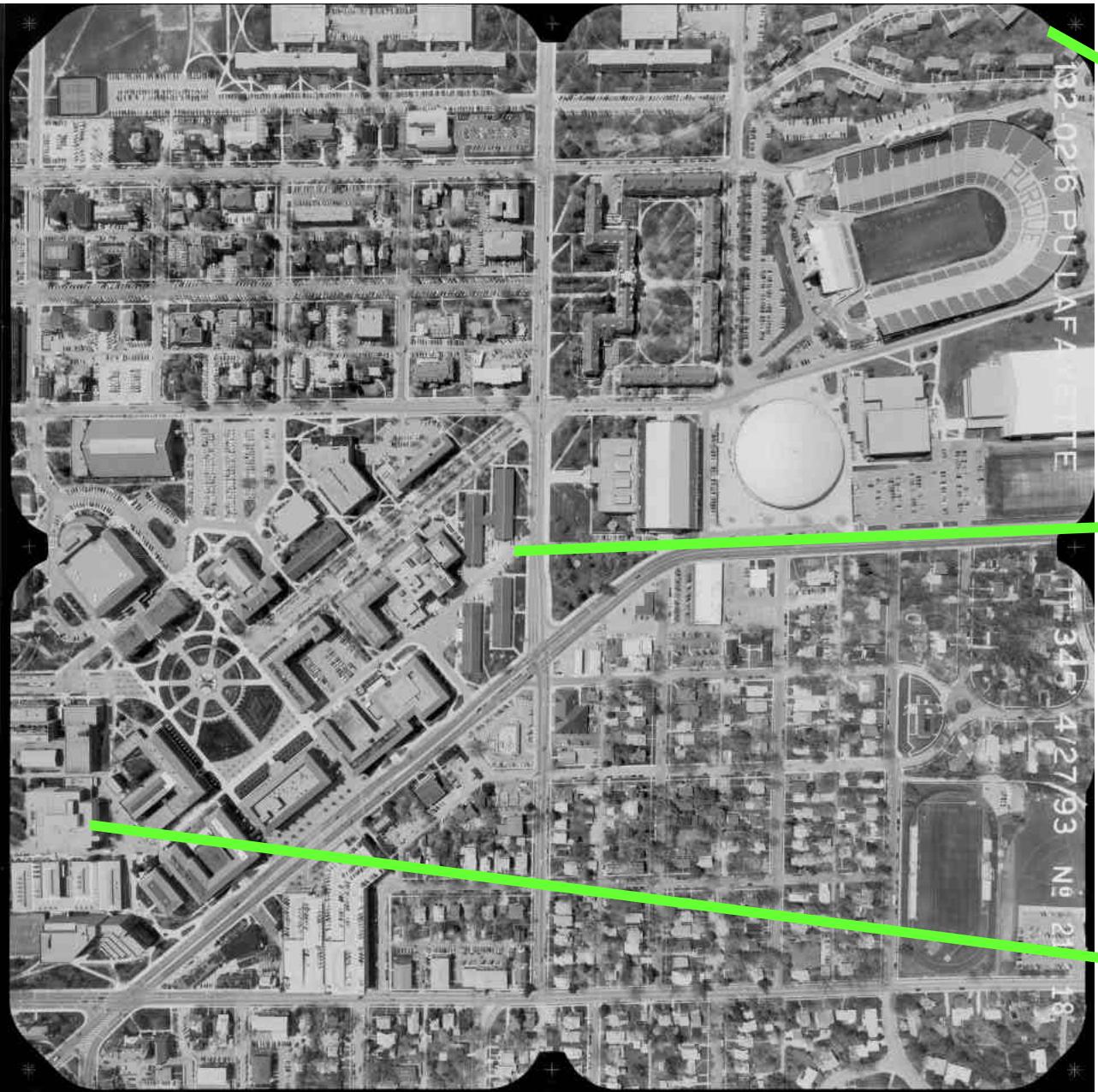
# International Society for Photogrammetry and Remote Sensing

- Commission I: Sensors, Platforms, and Imagery
- Commission II: Systems for Data Processing, Analysis, and Representation
- **Commission III: Theory and Algorithms**
- Commission IV: Spatial Information Systems and Digital Mapping
- Commission V: Close-Range Vision Technology
- Commission VI: Education and Communication
- Commission VII: Resource and Environmental Monitoring

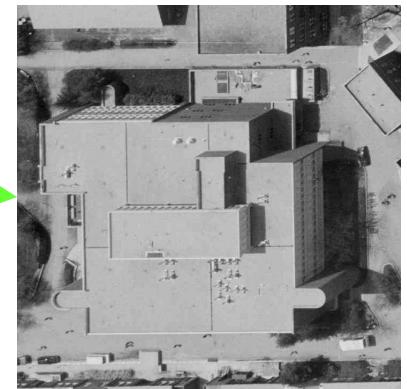


Commission III  
Symposium  
2002 Graz,  
Austria

Congress 2004  
Istanbul,  
Turkey

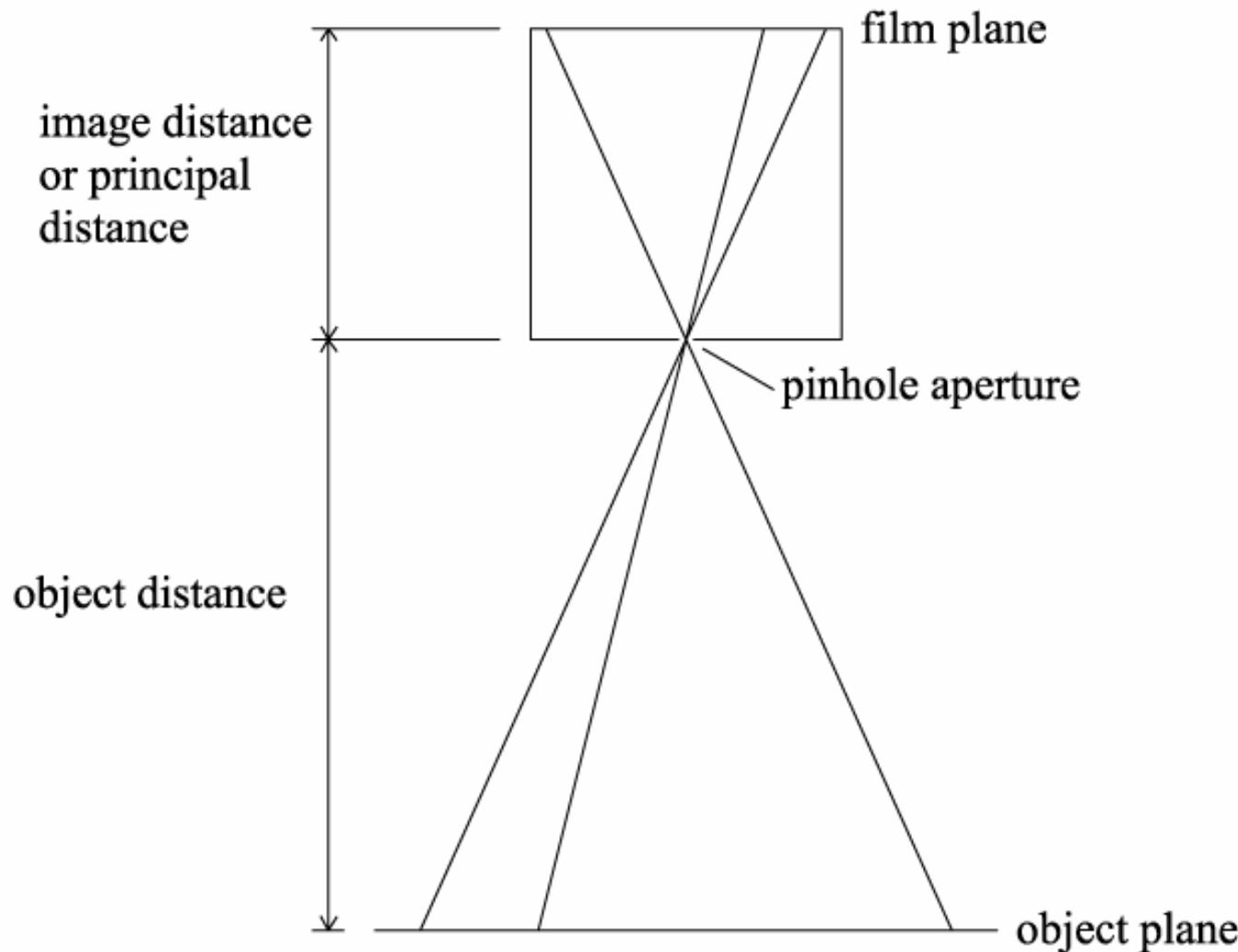


Relief Displacement

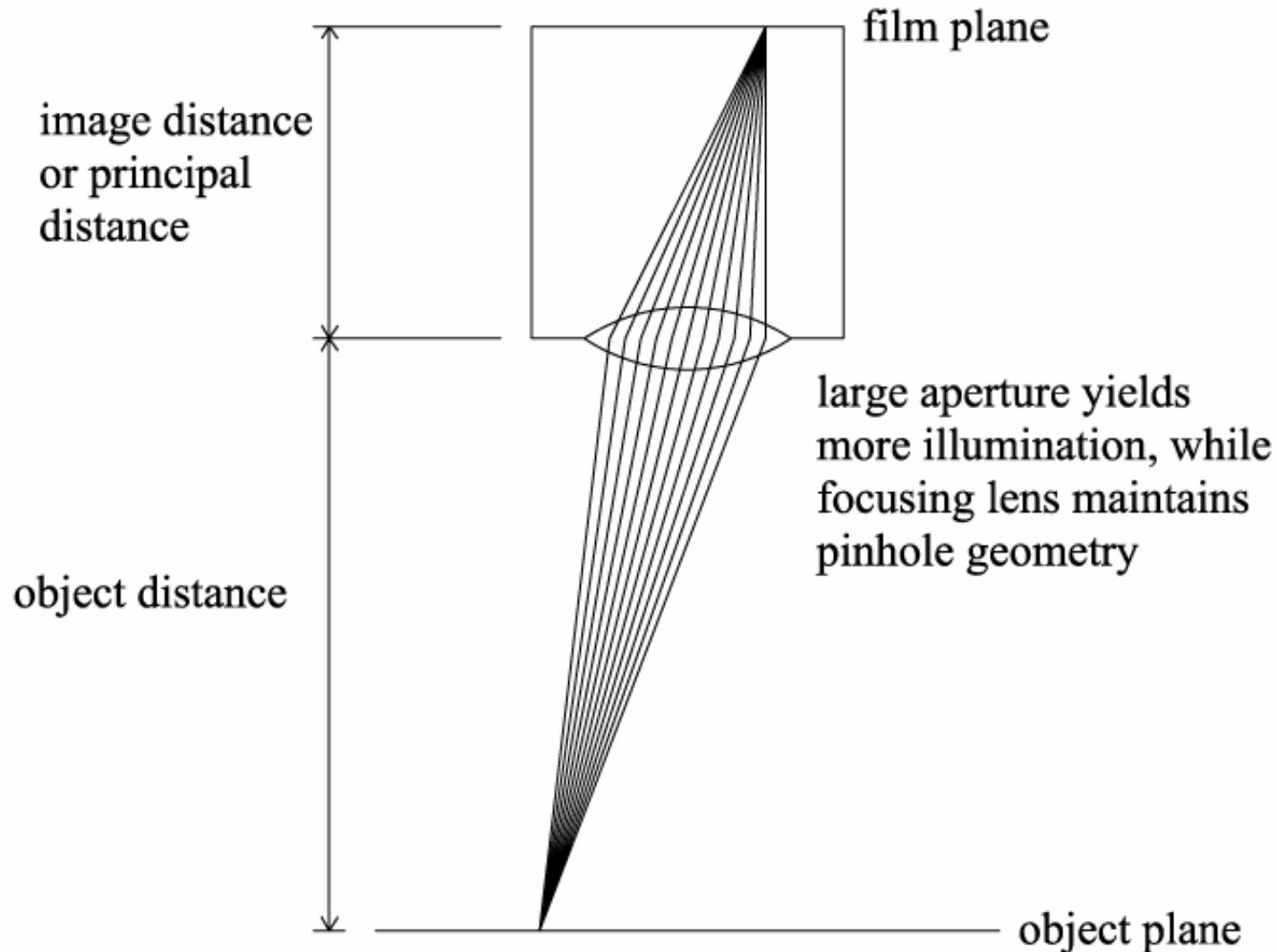


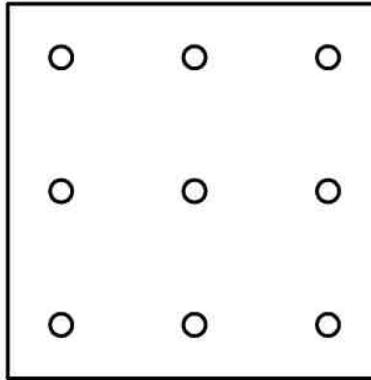
Note: nominal scale is the same everywhere in the image

# Frame Geometry



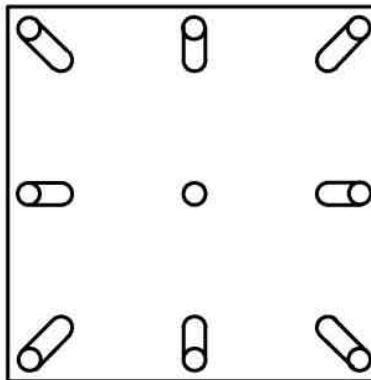
# Frame Geometry with Lens for Large Aperture



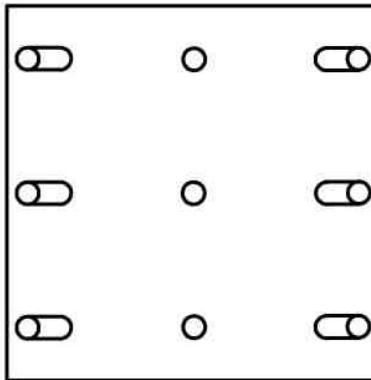


## Relief Displacement

Layout of vertically extended objects within an image



Relief displacement as found in *frame* imagery, entire image captured at same instant, relief displacement is always *radial* with respect to the *nadir point*



Relief displacement as found in *pushbroom* imagery, the image is built up *over time* by the platform motion, relief displacement only exists *within a line*. It is still radial with respect to the nadir point, but there is a different nadir point *for every line*. Therefore the only component of relief displacement is *cross-track*, there is no *along-track* component. (platform motion is up/down)

# Relief Displacement for Nadir Imagery

Ideal geometry: nadir imagery, flat terrain

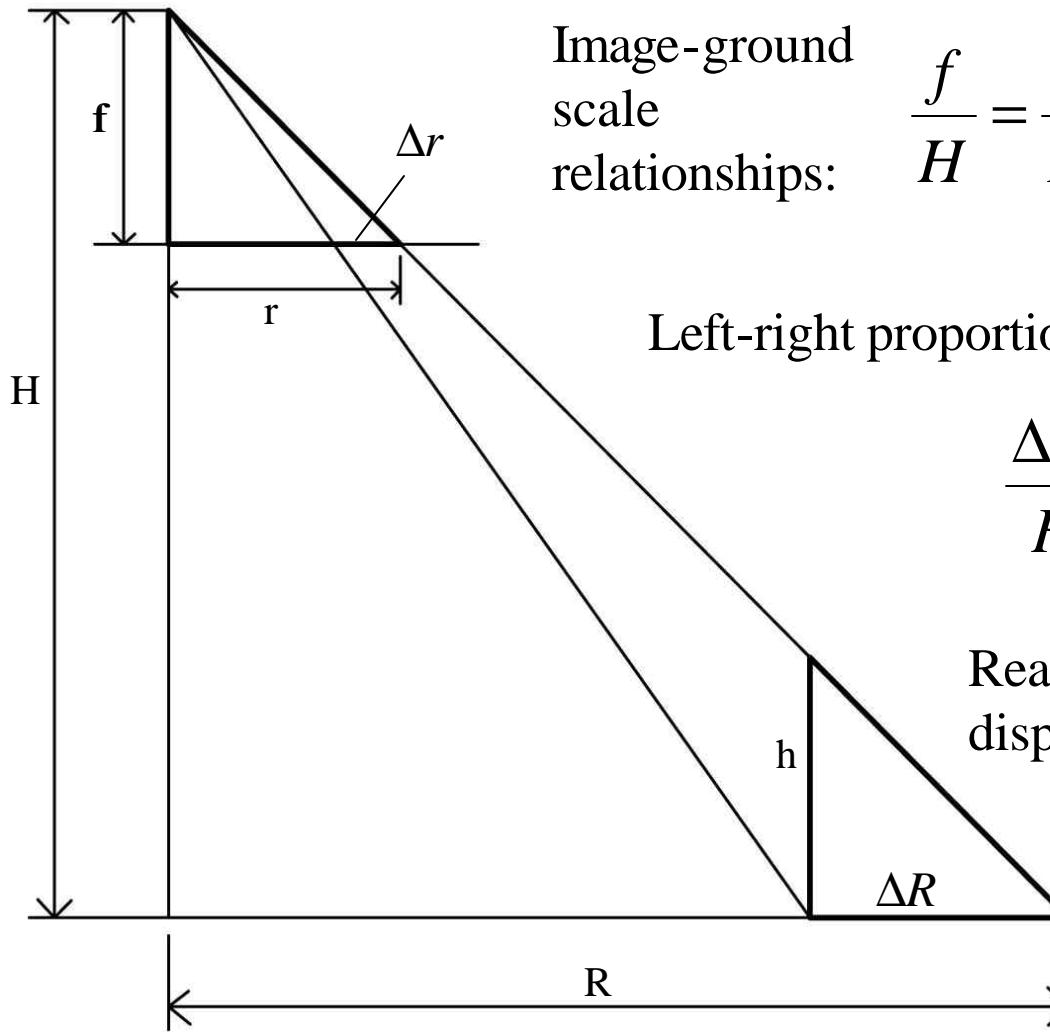


Image-ground  
scale  
relationships:

$$\frac{f}{H} = \frac{r}{R} = \frac{\Delta r}{\Delta R} = \text{scale}$$

Left-right proportionalities:

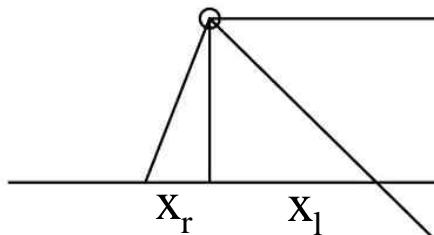
$$\frac{\Delta R}{R} = \frac{\Delta r}{r} = \frac{h}{H}$$

Rearrange for classic relief  
displacement formula:

$$h = \frac{\Delta r}{r} H$$

# Parallax: apparent change in position due to change in view location (sometimes called disparity)

Base = B



$$\text{parallax} = p = x_l - x_r$$

$$\frac{B}{H} = \frac{p}{f}$$

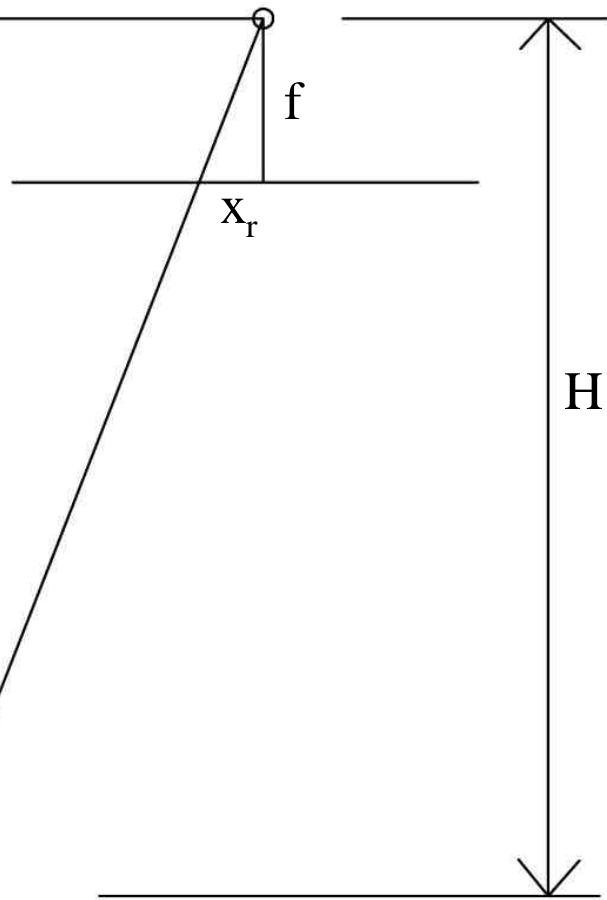
$$H = \frac{B}{p} f$$

Object distance  $\sim 1/p$

$\Rightarrow$  big distance : small parallax

$\Rightarrow$  small distance : big parallax

$$\frac{dp}{dH} = -fBH^{-2} = -\left(\frac{f}{H}\right)\frac{B}{H} = -(scale) \frac{B}{H} \Rightarrow \text{Rate of change of parallax with respect to distance } \sim \text{scale and } B/H$$



L



R

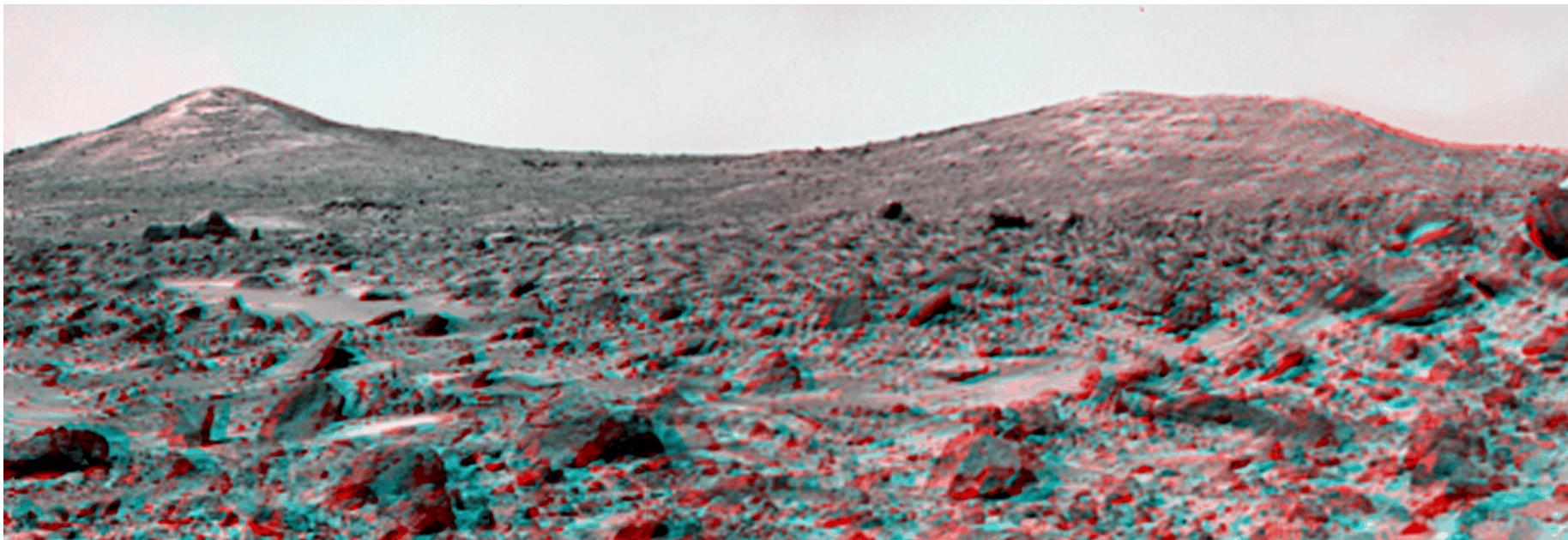


R



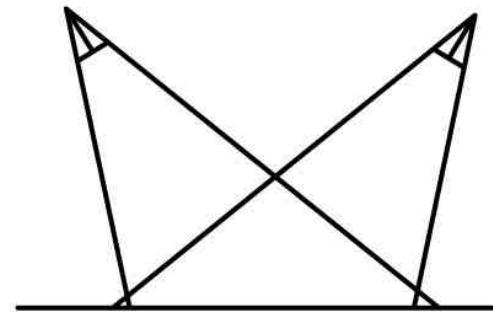
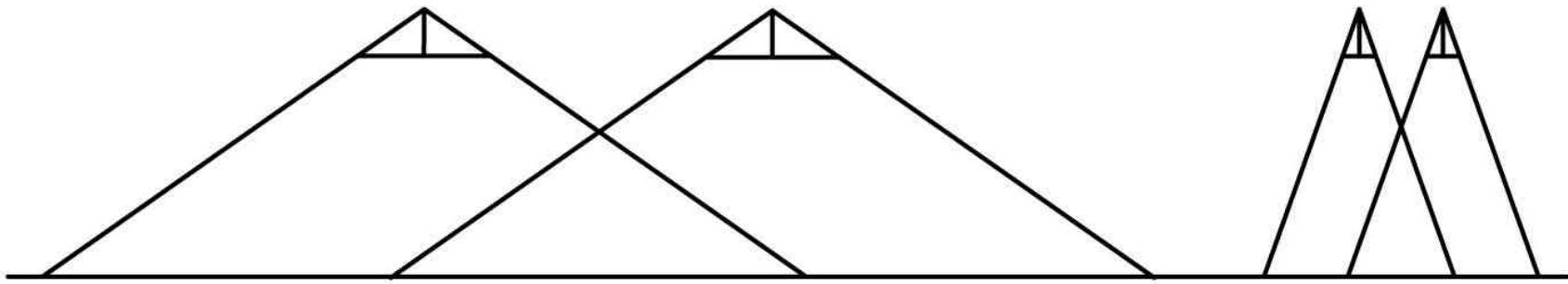
Near point (top of tank) makes a larger excursion between the left and right exposure, compared to the base of the tank (larger parallax or larger disparity). This disparity can be processed by our eyes to sense depth. A stereo cursor can be placed on an object to measure 3D coordinates delineate 3D features. If image B/H is greater than our eye's b/h, then we sense *vertical exaggeration*. This changes the appearance, but does not hurt measurement accuracy (in fact it helps).

Anaglyph Stereo of Mars scene shows greater disparity or parallax in foreground and less in the background or far distance



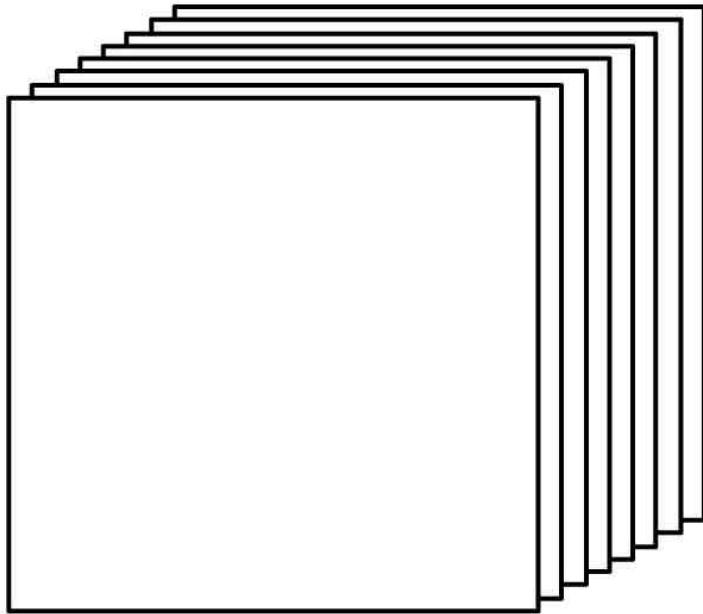
Wide angle and given overlap  
yields large B/H ratio

Narrow angle and same overlap  
yields small B/H ratio



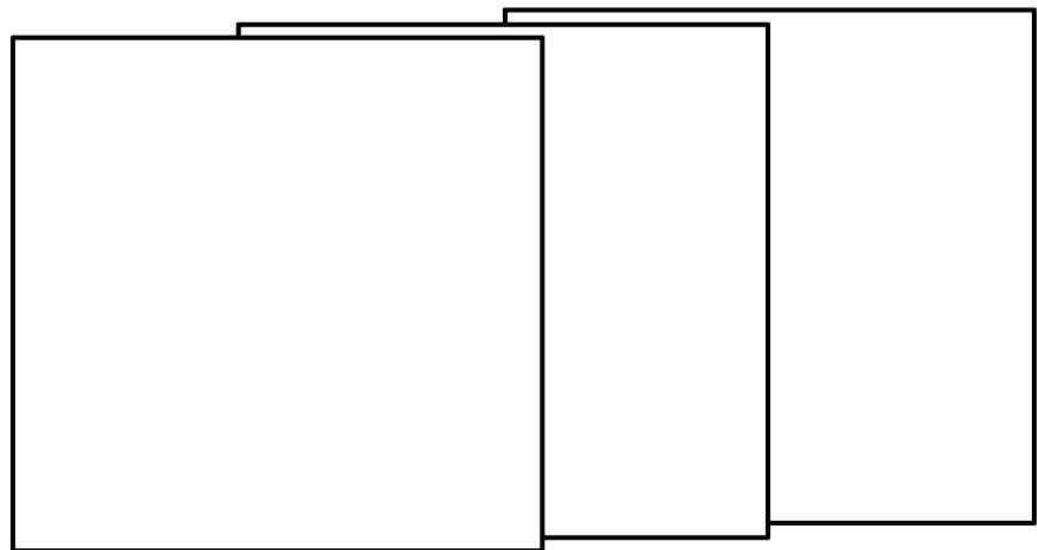
Can compensate for narrow angle camera by  
introducing strong convergence angle thus  
restoring favorable B/H ratio

High frame rate motion imagery =  
short baseline or small B/H (between  
adjacent images)



Correspondence is easy, since small  
displacements and parallaxes between  
adjacent images, for point tracking or  
optical flow, but determination of  
heights is weak (unless you extend  
over many frames)

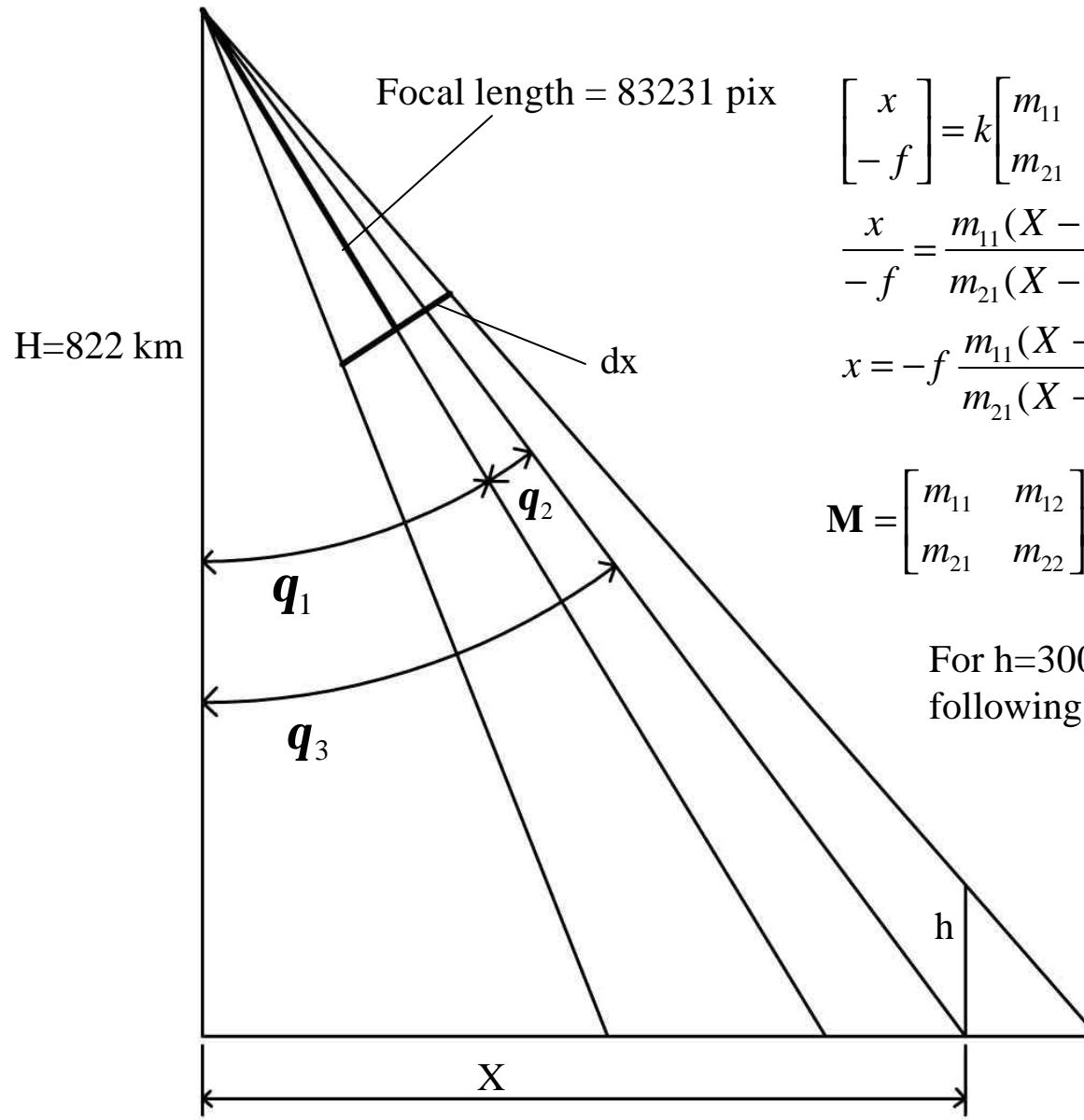
Conventional aerial imagery = long  
baseline or large B/H



Correspondence can be a challenge if  
large parallaxes, but determination of  
heights is strong

(X<sub>L</sub>, Z<sub>L</sub>)

## SPOT Off-Nadir Relief Displacement



Focal length = 83231 pix

$$\begin{bmatrix} x \\ -f \end{bmatrix} = k \begin{bmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{bmatrix} \begin{bmatrix} X - X_L \\ Z - Z_L \end{bmatrix}$$

$$\frac{x}{-f} = \frac{m_{11}(X - X_L) + m_{12}(Z - Z_L)}{m_{21}(X - X_L) + m_{22}(Z - Z_L)}$$

$$x = -f \frac{m_{11}(X - X_L) + m_{12}(Z - Z_L)}{m_{21}(X - X_L) + m_{22}(Z - Z_L)}$$

$$\mathbf{M} = \begin{bmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{bmatrix} = \begin{bmatrix} \cos q_1 & \sin q_1 \\ -\sin q_1 & \cos q_1 \end{bmatrix}$$

For h=300m, theta-2=2 deg, we have the following values for theta-1 and dx:

$q_1$	$dx$
10 deg	6.2 pix
20 deg	10.6 pix
27 deg	13.0 pix

Relief displacement for off-nadir SPOT is significant