# A Decision Model for Psychophysics 

Reading: Macmillan \& Creelman, Chaps. 1 \& 2

## Three Things to Learn

- Procedure

What are the stimuli?

- How do you present them?
- What are the responses?
- How do you organize the data?
- Model
- What are the assumptions?
- What is the model based on these assumptions?
- Data Processing
- How do you process the data?
- What are the results (e.g., threshold)?


## Introduction to Signal

## Detection Theory (SDT)

- Tanner \& Swets, 1954
- Key Properties of SDT
- Noise in perception

Probabilistic / stochastic approach
$\bullet$ Decision process (a priori info, bias)
Experimental procedure
Popular in literature

## Why Do We Care About SDT?

■ It provides a means to separate decision processes (e.g., bias) from perception.

- We will develop a decision model for psychophysics


## The Procedure for

## One-Interval (1-I) Experiments

- Name:

One-Interval, Two-Alternatives (1I 2A)

- Also known as the "yes-no" experiment (see Macmillan\&Creelman's book)
- There are two stimuli $\mathrm{S}_{\mathrm{i}}(\mathrm{i}=1,2)$; e.g., $-\mathrm{S}_{1}=$ "softer tone", $\mathrm{S}_{2}=$ "louder tone" $\bullet S_{1}=$ "softer spring", $S_{2}="$ harder spring" - $\mathrm{S}_{1}=$ "new face", $\mathrm{S}_{2}=$ "old face" (M\&C) $\bullet S_{1}="$ noise", $S_{2}=$ "signal embedded in noise"


## (cont.)

- On each trial, $\mathrm{S}_{\mathbf{i}}$ is presented with an a priori probability of $P\left(S_{i}\right)$, where $P\left(S_{1}\right)+P\left(S_{2}\right)=1$
- There are two admissible responses $\mathrm{R}_{\mathrm{j}}(\mathrm{j}=1,2)$; e.g.,
$\rightarrow \mathbf{R}_{1}=$ "softer tone", $\mathbf{R}_{2}="$ louder tone"
$\rightarrow R_{1}=" 1 ", R_{2}=" 2 "$
$\forall R_{1}=" n o ", R_{2}=" y e s "$ (hence "yes-no" exp.)
- For simplicity, we assume that $R_{1}$ is the correct response to $S_{1}$, and $R_{2}$ is the correct response to $S_{2}$
- Trial-by-trial correct-answer feedback is optional


## Data from a 1-I Experiment

|  | $\mathrm{R}_{1}$ | $\mathbf{R}_{2}$ |
| :---: | :---: | :---: |
| $\mathrm{S}_{1}$ |  | $n_{12}$ <br> False alarms |
| $\mathbf{S}_{2}$ | $n_{21}$ <br> Misses | $n_{22}$ <br> Hits |

- $f\left(R_{1} \mid S_{1}\right)=n_{11} /\left(n_{11}+n_{12}\right)$ : frequency of responding $R_{1}$ given $S_{1}$. We use frequency to estimate probability.
- $\mathrm{P}\left(\mathrm{R}_{1} \mid \mathrm{S}_{1}\right)$ : probability of responding $\mathrm{R}_{1}$ given $\mathrm{S}_{1}$
- $p\left(\mathbf{R}_{1} \mid \mathbf{S}_{1}\right)$ : probability density function
- There are only two independent measures: $F$ and $H$.


## Three Examples

## (1)

(2)
(3)

|  |  | $\mathbf{R}_{1}$ |
| :---: | :---: | :---: |
| $\mathbf{R}_{\mathbf{2}}$ |  |  |
|  | $S_{1}$ | 48 |
| $S_{2}$ | 1 | 2 |
|  |  | 49 |
|  |  |  |


|  | $\mathbf{R}_{1}$ | $\mathbf{R}_{\mathbf{2}}$ |
| :---: | :---: | :---: |
|  | $S_{1}$ | 5 |
| $S_{2}$ | 45 |  |
| $S_{2}$ | 1 | 49 |
|  |  |  |


|  | $\mathbf{R}_{1}$ | $\mathbf{R}_{2}$ |
| :---: | :---: | :---: |
|  | 2 | 48 |
| $S_{1}$ | 2 | 49 |
| $S_{2}$ | 49 | 1 |

## In-Class Lab: 1-I Experiment

- Go to "Online Experiments"
- Go down to "Part II. Decision Model for Psychophysics"
- Go to "One-interval Experiment"
- Select "1. Curvature detection"


## Discussion of In-Class Demo

- Summarize the procedure
-What are the stimuli?
- How do you present them?
-What are the responses?
- How do you organize the data?
- Sample output

|  | $R 1$ | $R 2$ |
| :--- | ---: | ---: |
| S1 | 37 | 13 |
| S2 | 14 | 36 |
| $H=0.72$ |  |  |
| $F=0.26$ |  |  |
| $d^{\prime}=1.22$ |  |  |
| $c=0.03$ |  |  |

(Please write down your own results in a notebook)

