ECE-255
Final Exam
May/01/2012

Name: $\qquad$
(Please print clearly)
Student ID: $\qquad$

## INSTRUCTIONS

- This is a closed book, closed notes exam. Calculators are allowed.
- Carefully mark your multiple choice answers on the scantron form. Work on multiple choice problems and marked answers in the test booklet will not be graded. Nothing is to be on the seat beside you.
- When the exam ends, all writing is to stop. This is not negotiable. No writing while turning in the exam/scantron or risk an F in the exam.
- All students are expected to abide by the customary ethical standards of the university, i.e., your answers must reflect only your own knowledge and reasoning ability. As a reminder, at the very minimum, cheating will result in a zero on the exam and possibly an F in the course.
- Communicating with any of your classmates, in any language, by any means, for any reason, at any time between the official start of the exam and the official end of the exam is grounds for immediate ejection from the exam site and loss of all credit for this exercise.

1. A silicon sample at room temperature has an intrinsic carrier concentration of $n_{i}$ $=10^{10} \mathrm{~cm}^{-3}$. It is doped with $\mathrm{N}_{\mathrm{A}}=1 \times 10^{18}$ boron atoms $/ \mathrm{cm}^{3}$ and $\mathrm{N}_{\mathrm{D}}=6 \times 10^{12}$ arsenic atoms $/ \mathrm{cm}^{3}$. The electron mobility is measured as $\mu_{\mathrm{n}}=1000 \mathrm{~cm}^{2} / \mathrm{V} \cdot \mathrm{s}$. What are the electron and hole concentration in this material and electron current density when an external field of $\mathrm{E}=100 \mathrm{~V} / \mathrm{cm}$ is applied? $\left(\mathrm{q}=1.6 \times 10^{-19} \mathrm{C}\right)$
(1) $\mathrm{p}=1 \times 10^{18} / \mathrm{cm}^{3} ; \mathrm{n}=6 \times 10^{12} / \mathrm{cm}^{3} ; \mathrm{j}_{\mathrm{n}}=9.6 \times 10^{-2} \mathrm{~A} / \mathrm{cm}^{2}$
(2) $\mathrm{p}=1 \times 10^{10} / \mathrm{cm}^{3} ; \mathrm{n}=6 \times 10^{12} / \mathrm{cm}^{3} ; \mathrm{j}_{\mathrm{n}}=1.6 \times 10^{-4} \mathrm{~A} / \mathrm{cm}^{2}$
(3) $\mathrm{p}=6 \times 10^{12} / \mathrm{cm}^{3} ; \mathrm{n}=1 \times 10^{18} / \mathrm{cm}^{3} ; \mathrm{j}_{\mathrm{n}}=1.6 \times 10^{4} \mathrm{~A} / \mathrm{cm}^{2}$
(4) $\mathrm{p}=1 \times 10^{18} / \mathrm{cm}^{3} ; \mathrm{n}=100 / \mathrm{cm}^{3} ; \mathrm{j}_{\mathrm{n}}=1.6 \times 10^{-12} \mathrm{~A} / \mathrm{cm}^{2}$
(5) $\mathrm{p}=1 \times 10^{18} / \mathrm{cm}^{3} ; \mathrm{n}=100 / \mathrm{cm}^{3} ; \mathrm{j}_{\mathrm{n}}=1.6 \times 10^{4} \mathrm{~A} / \mathrm{cm}^{2}$
(6) None of the above
2. For the diode circuit below, determine the current, I (indicated in the graph), using the constant voltage model with Von $=0.7 \mathrm{~V}$.

(1) $I=0 A$
(2) $I=0.3 \mathrm{~mA}$
(3) $I=2.7 \mathrm{~mA}$
(4) $I=3.3 \mathrm{~mA}$
(5) $I=3.7 \mathrm{~mA}$
(6) None of the above
3. In the circuit below, the Zener diode has a breakdown voltage $\mathrm{V}_{\mathrm{Z} 0}=8.0 \mathrm{~V}$ and a measurement has shown that $\mathrm{V}_{\mathrm{Z}}=8.2 \mathrm{~V}$ when $\mathrm{I}_{\mathrm{Z}}=20 \mathrm{~mA}$. What is the value of $\mathrm{V}_{\text {out }}$ when $\mathrm{R}_{\mathrm{L}}$ is infinitely large?

(1) $\mathrm{V}_{\text {out }}=0 \mathrm{~V}$
(2) $\mathrm{V}_{\text {out }}=8.2 \mathrm{~V}$
(3) $\mathrm{V}_{\text {out }}=8.8 \mathrm{~V}$
(4) $V_{\text {out }}=8.4 \mathrm{~V}$
(5) $\mathrm{V}_{\text {out }}=8.0 \mathrm{~V}$
(6) None of the above
4. Determine the collector current, Ic, for the following BJT circuit. $\beta_{\mathrm{F}}=99, \mathrm{~V}_{\mathrm{BE}}(\mathrm{on})=0.7 \mathrm{~V}$.

(1) Ic $=2 \mathrm{~mA}$
(2) $\mathrm{Ic}=1.98 \mathrm{~mA}$
(3) $\mathrm{Ic}=2.15 \mathrm{~mA}$
(4) $\mathrm{Ic}=0.02 \mathrm{~mA}$
(5) Ic $=1.435 \mathrm{~mA}$
(6) None of the above
5. For the MOS circuit shown below, what is the output voltage, $\mathrm{V}_{0}$ ? $\lambda=0, \mathrm{~V}_{\mathrm{TN}}=1 \mathrm{~V}, \mathrm{~K}_{\mathrm{N}}=0.3 \mathrm{~mA} / \mathrm{V}^{2}$
(1) $V_{o}=2 V$
(2) $V_{o}=2.5 \mathrm{~V}$
(3) $\mathrm{V}_{\mathrm{o}}=3 \mathrm{~V}$
(4) $V_{o}=3.5 \mathrm{~V}$
(5) $\mathrm{V}_{\mathrm{o}}=4 \mathrm{~V}$
(6) None of the above

6. Determine the voltage gain, input resistance and output resistance (both are indicated in the graph) of the amplifier circuit shown below.
$\beta_{o}=80, V_{A}=\propto, V_{T}=25 \mathrm{mV}$.

(1) $\mathrm{A}_{\mathrm{v}} \approx 1 ; \mathrm{R}_{\text {in }}=204.5 \mathrm{k} \Omega ; \mathrm{R}_{\text {out }} \approx 37 \Omega$
(2) $\mathrm{A}_{\mathrm{v}} \approx 100 ; \mathrm{R}_{\text {in }}=20 \mathrm{k} \Omega ; \mathrm{R}_{\text {out }} \approx 37 \Omega$
(3) $\mathrm{A}_{\mathrm{v}} \approx-100 ; \mathrm{R}_{\text {in }}=2 \mathrm{k} \Omega ; \mathrm{R}_{\text {out }} \approx 2.5 \mathrm{k} \Omega$
(4) $\mathrm{A}_{\mathrm{v}} \approx 1 ; \mathrm{R}_{\text {in }}=400 \mathrm{k} \Omega ; \mathrm{R}_{\text {out }} \approx 25 \Omega$
(5) $\mathrm{A}_{\mathrm{v}} \approx 100 ; \mathrm{R}_{\text {in }}=1 \mathrm{k} \Omega ; \mathrm{R}_{\text {out }} \approx 5 \mathrm{k} \Omega$
(6) None of the above
7. Determine the input resistance, $\mathrm{R}_{\mathrm{i}}$, for the amplifier circuit below (currents for $Q_{2}$ and $Q_{3}$ are indicated in the figure, and it needs to be calculated for $Q_{1}$ ). Assume $\beta_{0}=100, \mathrm{~V}_{\mathrm{A}}=\infty, \mathrm{V}_{\mathrm{BE}}(\mathrm{on})=0.7 \mathrm{~V}, \mathrm{~V}_{\mathrm{T}}=25 \mathrm{mV}$ for all BJTs , and $\mathrm{V}+=5 \mathrm{~V}$.

(1) $\approx 500 \mathrm{k} \Omega$
(2) $\approx 5 \mathrm{k} \Omega$
(3) $\approx 250 \mathrm{k} \Omega$
(4) $\approx 1.5 \mathrm{Mk} \Omega$
(5) $\approx 1 \mathrm{M} \Omega$
(6) None of the above
8. What are the common-mode gain $\left(\left|\mathrm{Av}_{\mathrm{c}}\right|\right)$ and differential mode gain $\left(\left|A v_{\mathrm{d}}\right|\right)$ for the circuit shown below? Assuming $\beta_{0} \gg 1$.

(1) $\left|\mathrm{Av}_{\mathrm{c}}\right| \approx 0.1 ;\left|A \mathrm{~A}_{\mathrm{d}}\right| \approx 10$
(2) $\left|A \mathrm{Av}_{\mathrm{c}}\right| \approx 0.1 ;\left|\mathrm{Av}_{\mathrm{d}}\right| \approx 33$
(3) $\left|A \mathrm{v}_{\mathrm{c}}\right| \approx 0.2 ;\left|\mathrm{Av}_{\mathrm{d}}\right| \approx 50$
(4) $\left|A v_{c}\right| \approx 0.1 ;\left|A v_{\mathrm{d}}\right| \approx 25$
(5) $\left|A v_{\mathrm{c}}\right| \approx 25 ;\left|A v_{\mathrm{d}}\right| \approx 0.1$
(6) None of the above
9. Choose the value of $\mathrm{C}_{1}$ so that it can be neglected at frequencies larger than the low cutoff frequency, $f_{L}=10 \mathrm{KHz}$. We use $C_{1} \geq 10 \frac{1}{\omega_{L} R_{1 s}}$ as the design rule.

(1) $\mathrm{C}_{1}>79 \mathrm{nF}$
(2) $\mathrm{C}_{1}>72.3 \mathrm{pF}$
(3) $\mathrm{C}_{1}>106 \mathrm{pF}$
(4) $\mathrm{C}_{1}>0.0178 \mathrm{nF}$
(5) $\mathrm{C}_{1}>0.178 \mathrm{nF}$
(6) None of the above
10. For the amplifier circuit shown below, calculate upper- cutoff frequency, $f_{H}$.

(1) $\sim 94 \mathrm{MHz}$
(2) $\sim 15 \mathrm{MHz}$
(3) $\sim 35 \mathrm{MHz}$
(4) $\sim 50 \mathrm{MHz}$
(5) $\sim 10 \mathrm{MHz}$
6) Non of the above
11. For the amplifier circuit shown below $\mathrm{I}_{\mathrm{B}}=$ ?

Assume $\beta=180, \mathrm{~V}_{\mathrm{A}}=\infty$, and $\mathrm{V}_{\mathrm{BE}}(\mathrm{on})=0.7 \mathrm{~V}$

(1) $\sim 87 \mu \mathrm{~A}$
(2) $\sim 182 \mu \mathrm{~A}$
(3) $\sim 7.3 \mu \mathrm{~A}$
(4) $\sim 1.4 \mathrm{~mA}$
(5) $100 \mu \mathrm{~A}$
(6) None of the above
12. Mid-band gain $\left(\mathrm{A}_{\text {mid }}\right)$, lower cutoff frequency $\left(\omega_{\mathrm{L}}\right)$, and higher cutoff frequency $\left(\omega_{\mathrm{H}}\right)$ for the amplifier transfer function given below are

$$
A_{v}(s)=\frac{4 \times 10^{8} s^{2}}{(s+1)(s+2)(s+1000)(s+2000)}
$$

(1) $\mathrm{A}_{\text {mid }}=4 \times 10^{8}, \omega_{\mathrm{L}}=2 \mathrm{rad} / \mathrm{s}, \omega_{\mathrm{H}}=1000 \mathrm{rad} / \mathrm{s}$
(2) $\mathrm{A}_{\text {mid }}=200, \omega_{\mathrm{L}}=1 \mathrm{rad} / \mathrm{s}, \omega_{\mathrm{H}}=816.5 \mathrm{rad} / \mathrm{s}$
(3) $\mathrm{A}_{\mathrm{mid}}=400, \omega_{\mathrm{L}}=2.24 \mathrm{rad} / \mathrm{s}, \omega_{\mathrm{H}}=1000 \mathrm{rad} / \mathrm{s}$
(4) $\mathrm{A}_{\mathrm{mid}}=200, \omega_{\mathrm{L}}=2.24 \mathrm{rad} / \mathrm{s}, \omega_{\mathrm{H}}=2000 \mathrm{rad} / \mathrm{s}$
(5) $\mathrm{A}_{\text {mid }}=200, \omega_{\mathrm{L}}=2.24 \mathrm{rad} / \mathrm{s}, \omega_{\mathrm{H}}=894 \mathrm{rad} / \mathrm{s}$
(6) None of the above
13. What is the configuration of the multi-stage amplifier shown below?

(1) CB-CC
(2) CE-CC
(3) CB-CB
(4) CC-CC
(5) CB-CE
(6) None of the above
14. What is $\mathrm{V}_{\mathrm{o}}$ ? if $\mathrm{V}_{\mathrm{i}}=0.725 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{s}}=10^{-14} \mathrm{~A}$ (Assume $\mathrm{V}_{\mathrm{T}}=25 \mathrm{mV}$ )

(1) 0 V
(2) -0.725 V
(3) -3.9 V
(4) -0.1 V
(5) -2.5 V
(6) None of the above
15. For the MOS circuit shown below, $\mathrm{I}_{\mathrm{D}}=$ ?

## $\mathrm{V}_{\mathrm{TN}}=1 \mathrm{~V}, \mathrm{~K}_{\mathrm{N}}=0.1 \mathrm{~mA} / \mathrm{V}^{2}$


(1) 0.1 mA
(2) 0.4 mA
(3) 0.5 mA
(4) 0.2 mA
(5) 1 mA
(6) None of the above
16. Figure below shows a cascode MOSFET, what is the mid-band gain $\left(\mathrm{A}_{\mathrm{v}}=\mathrm{V}_{\mathrm{o}} / \mathrm{V}_{\mathrm{i}}\right)$ ? Assume $\mathrm{g}_{\mathrm{m}}=2 \mathrm{~mA} / \mathrm{V}$ and $\lambda=0$ for both transistors

(1) -20
(2) -400
(3) -2
(4) -100
(5) -6.67
(6) None of the above
17. Which one of the current gain $\left(\mathrm{A}_{\mathrm{i}}\right)$ frequency response curves belong to the amplifier shown below?

(1)


(2)

(5) Circuit cannot provide any current gain
(3)

(6) None of the above
18.For the amplifier circuit shown below estimated value of $f_{L}$ is? For BJT assume $\beta=150, \mathrm{~V}_{\mathrm{A}}=75 \mathrm{~V}, \mathrm{~V}_{\mathrm{BE}}(\mathrm{on})=0.7, \mathrm{~V}_{\mathrm{T}}=25 \mathrm{mV}$.

(1) $\sim 1 \mathrm{kHz}$
(2) $\sim 10 \mathrm{~Hz}$
(3) $\sim 0.64 \mathrm{~Hz}$
(4) 0 Hz
(5) $\sim 2.5 \mathrm{~Hz}$
(6) None of the above
19. What is the value of output impedance (Ro) for the current mirror shown below? Assume $\beta=\infty, \mathrm{V}_{\mathrm{BE}}(\mathrm{ON})=0.7 \mathrm{~V}, \mathrm{~V}_{\mathrm{A}}=75 \mathrm{~V}$. Two transistors are identical

(1) $40 \mathrm{k} \Omega$
(2) $\infty$
(3) $174 \mathrm{k} \Omega$
(4) $81 \mathrm{k} \Omega$
(5) $500 \mathrm{k} \Omega$
(6) None of the above
20. What is the voltage gain $\left(\mathrm{v}_{0} / \mathrm{v}_{\mathrm{i}}\right)$ for the amplifier below? Assume the MOSFET Q points are $(2 \mathrm{~mA}, 7.5 \mathrm{~V}), \mathrm{K}_{\mathrm{n}}=1 \mathrm{~mA} / \mathrm{V}^{2}$, and $\lambda=0$

(1) -7.8
(2) -7.61
(3) -540
(4) -25
(5) gain is zero since we ignored the channel length modulation
(6) None of the above

## DIODE EQUATIONS



$$
i_{D}=I_{S}\left[\exp \left(\frac{v_{D}}{n V_{T}}\right)-1\right] \quad V_{T}=\frac{k T}{q}
$$

$$
C_{j}=\frac{C_{j o} A}{\sqrt{1-\frac{v_{D}}{\phi_{j}}}}
$$

$$
C_{D}=\frac{I_{D}}{V_{T}} \tau_{T}
$$



BJT SMALL-SIGNAL MODEL PARAMETER RELATIONSHIPS $\left(\beta_{o} \cong \beta_{F}\right)$

$$
g_{m}=\frac{I_{C}}{V_{T}} \cong 40 I_{C} \quad \beta_{o}=g_{m} r_{\pi} \quad r_{o}=\frac{V_{A}+V_{C E}}{I_{C}} \cong \frac{V_{A}}{I_{C}} \quad \mu_{f}=g_{m} r_{o} \quad C_{\pi}=g_{m} \tau_{F} \quad \omega_{T}=\frac{g_{m}}{C_{\pi}+C_{\mu}}
$$

## LARGE SIGNAL MODEL EQUATIONS - NMOS TRANSISTOR

Triode (Linear) Region ( $v_{G S}>V_{T N}$ and $v_{D S} \leq v_{G S}-V_{T N}$ )

$$
i_{D}=K_{n}\left(v_{G S}-V_{T N}-\frac{v_{D S}}{2}\right) v_{D S} \quad i_{G}=0 \quad i_{S}=i_{D} \quad K_{n}=K_{n}^{\prime} \frac{W}{L}
$$



Active (Saturation) Region $\left(v_{G S}>V_{T N}\right.$ and $\left.v_{D S} \geq v_{G S}-V_{T N}\right)$

$$
\begin{gathered}
i_{D}=\frac{K_{n}}{2}\left(v_{G S}-V_{T N}\right)^{2}\left(1+\lambda v_{D S}\right) \quad i_{G}=0 \quad i_{S}=i_{D} \quad K_{n}=K_{n}^{\prime} \frac{W}{L} \\
V_{T N}=V_{T O}+\gamma\left(\sqrt{v_{S B}+2 \phi_{f}}-\sqrt{2 \phi_{f}}\right)
\end{gathered}
$$

## FET SMALL-SIGNAL MODEL PARAMETER RELATIONSHIPS

$$
g_{m}=\frac{2 I_{D}}{V_{G S}-V_{T N}} \cong \sqrt{2 K_{n} I_{D}} \quad r_{o}=\frac{1+\lambda V_{D S}}{\lambda I_{D}} \cong \frac{1}{\lambda I_{D}} \quad \mu_{f}=g_{m} r_{o} \quad \omega_{T}=\frac{g_{m}}{C_{G S}+C_{G D}}
$$

Low frequency pole location for a transfer function with $n$ poles and zeros

$$
\omega_{L} \cong \sqrt{\sum_{n} \omega_{P n}^{2}-2 \Sigma \omega_{Z}^{2} n^{2}}
$$

High frequency pole location for a transfer function with n poles and zeros

$$
\omega_{H} \cong \frac{1}{\sqrt{\sum_{n} \frac{1}{\omega_{P n}}{ }^{2}-2 \sum \frac{1}{\omega_{Z n}}{ }^{2}}}
$$

Approximate equation for finding $\omega_{\mathrm{L}}$ using short-circuit time constant method

$$
\omega_{L} \cong \sum_{i=1}^{n} \frac{1}{R_{i S} C_{i}}
$$

Approximate equation for finding $\omega_{H}$ using open-circuit time constant method

$$
\omega_{H} \cong \frac{1}{\sum_{i=1}^{m} R_{i o} C_{i}}
$$

