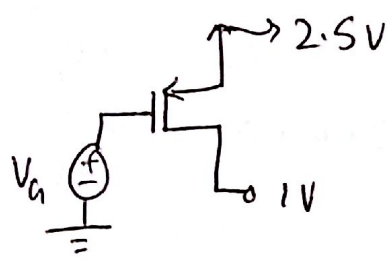


ECE 255 HW 8

5.41

$V_{tp} = -0.5V$
 $V_{G1} \in [0, 2.5] V$

$V_S = 2.5V$ $V_D = 1V$



$V_{SG1} > |V_{tp}| \rightarrow ON$

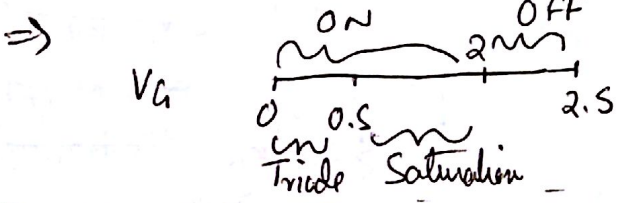
$2.5 - V_{G1} > 0.5$

$\Rightarrow V_{G1} < 2V \rightarrow ON$

$V_{DG1} \leq |V_{tp}| \rightarrow \text{Saturation region}$

$\Rightarrow 1 - V_{G1} \leq 0.5 \Rightarrow V_{G1} \geq 0.5 \rightarrow \text{Saturation}$

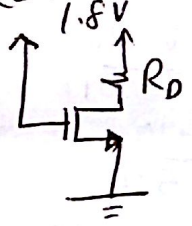
$V_{G1} < 0.5 \rightarrow \text{Triode}$



5.47

$k_n' = 0.4 mA/V^2$ $V_t = 0.5V$ $\lambda = 0$

$(\frac{W}{L})R_D = 1.5k\Omega$ at Edge of Saturation



$V_{G1} = 1.8V$

$V_S = 0V$

$V_D = 1.8 - I_D R_D$

At the edge of saturation

$V_{DS} = V_{GS} - V_t \Rightarrow 1.8 - I_D R_D = 1.8 - 0.5$

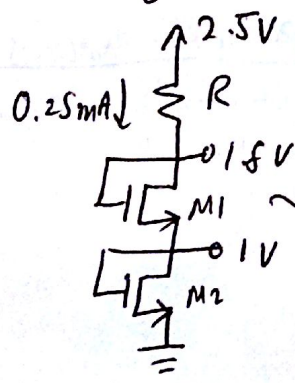
$\Rightarrow I_D R_D = 0.5 \Rightarrow R_D = \frac{0.5}{I_D} = \frac{0.5}{\frac{k_n' W}{2L} V_{ov}^2} = \frac{0.5 \times 2}{0.4 (\frac{W}{L}) (1.3)^2}$

$\Rightarrow \frac{W}{L} R_D = \frac{5 \times 2}{2 \times 1.69} = \frac{5}{3.4} \approx 1.5k\Omega //$

5.50

$V_t = 0.5V$

$M_n(\text{ox}) = 250 \mu A/V^2$, $\lambda = 0$ & $L_1 = L_2 = 0.25 \mu m$



$R = \frac{2.5 - 1.8}{0.25mA} = \frac{0.7}{0.25mA} = 2.8k\Omega$

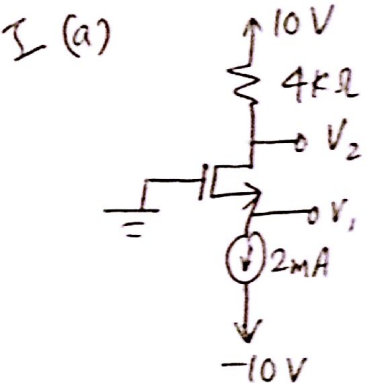
$I_{D1} = I_{D2} = 0.25mA$

$0.25mA = 250 \mu \frac{W}{L} (1.8 - 1 - 0.5)^2$

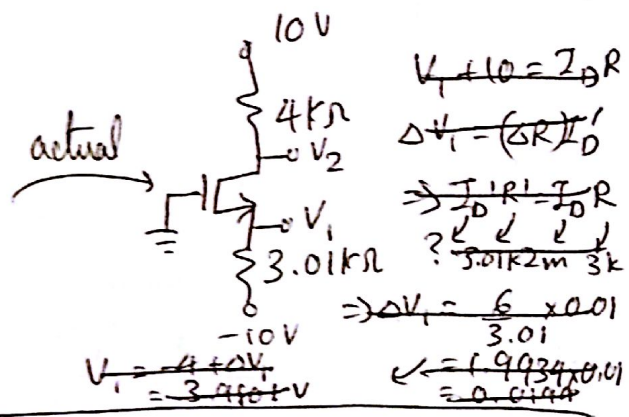
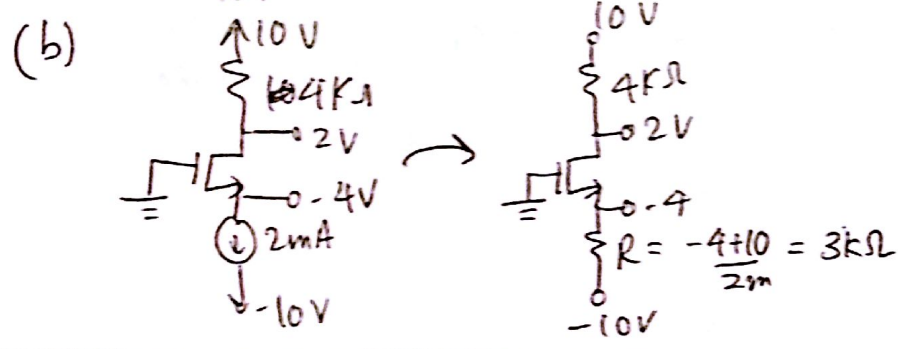
$\frac{1}{2} M = W (0.3)^2 \Rightarrow W_1 = \frac{1}{2 \times 0.09} = \frac{1}{0.18} \mu = 5.56 \mu m$

$0.25mA = 250 \mu \frac{W}{L} (1 - 0.5)^2 \Rightarrow W_2 = \frac{1}{2 \times 0.25} M = \frac{1}{0.5} M = 2 \mu m$

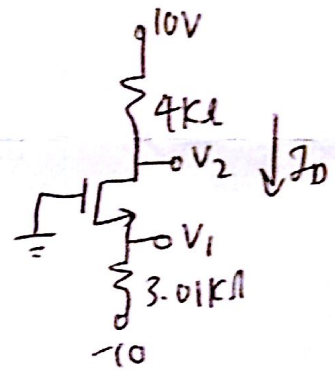
5.55 $|V_{t1}| = 2V$, $k'W/L = 1mA/V^2$ & $\lambda = 0$



$I_D = 2mA \Rightarrow 10 - V_2 = 8 \Rightarrow V_2 = 2V_{//}$
 Assume MOSFET in SAT ($V_{DS} = V_2 - V_1 = 6V > V_{OV} = 0 - (-4) - 2 = 2V$)
 $\Rightarrow 2m = \frac{1mA}{2} (0 - V_1 - 2)^2 \Rightarrow \pm 2 = 2 + V_1$
 as $V_{OV} > 0 \Rightarrow -V_1 - 2 > 0 \Rightarrow 2 + V_1 < 0 \Rightarrow 2 + V_1 = -2 \Rightarrow V_1 = -4V_{//}$



EXACT ANALYSIS

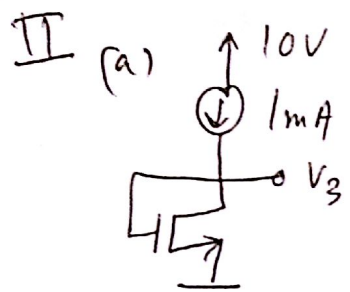


$V_2 = 10 - 4I_D$
 $V_1 = I_D(3.01) - 10$
 $I_D = \frac{k'W}{2L} V_{OV}^2 = \frac{1m}{2} (0 - V_1 - 2)^2$
 $I_D = \frac{1m}{2} (3.9972 - 2)^2 = 1.9944$
 $V_2 = 10 - 4I_D = 2.0223V_{//}$ (slight difference)

$\Rightarrow 0.5m(V_1 + 2)^2 = \frac{V_1 + 10}{3.01k}$
 $(V_1 + 2)^2 = \frac{V_1 + 10}{1.505}$
 $V_1^2 + 4 + 4V_1 - \frac{V_1}{1.505} - \frac{10}{1.505} = 0$
 $V_1^2 + 3.3355V_1 - 2.645 = 0$
 $V_1 = \frac{-3.3355 \pm \sqrt{11.1256 + 10.58}}{2} = \frac{-3.3355 \pm 4.6589}{2}$
 $V_1 = -3.9972V_{//}$ (The SAME)

- V_1 remains almost the same (increased by a small %). $V_1 = -4V_{//}$
 - But as $I_D \downarrow$ (as $I_D R = I_D' R'$, $I_D' = 1.9934mA$) $V_2 \uparrow$ considerably as compared to V_1
- $\Delta V_2 = 4k \Delta I_D = 0.0264 \Rightarrow V_2 = 2.0264V_{//}$

APPROXIMATE ANALYSIS



$$V_D = V_G \Rightarrow \text{SAT}^n$$

$$I_D = \frac{1m}{2} (V_3 - 2)^2 = 1mA$$

$$\Rightarrow 2 = (V_3 - 2)^2 \Rightarrow V_3 = +\sqrt{2} + 2 = 3.414V$$

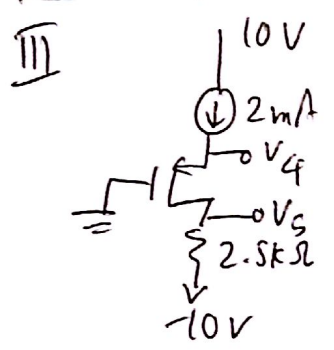
$$V_3 - 2 > 0 \rightarrow \text{ON}$$



$$R = \frac{10 - 3.414}{1m} = 6.586k\Omega \quad (6.65k\Omega \text{ approximation})$$

$$I_D' = \frac{6.586}{6.65} = 0.9904mA$$

$$\Rightarrow \Delta V_3 = -(\Delta I_D R + \Delta R I_D') \Rightarrow V_3 \text{ should approximately be the same}$$



$$V_S + 10 = 2.5k \cdot 2m$$

$$\Rightarrow V_S = -10 + 5 = -5V //$$

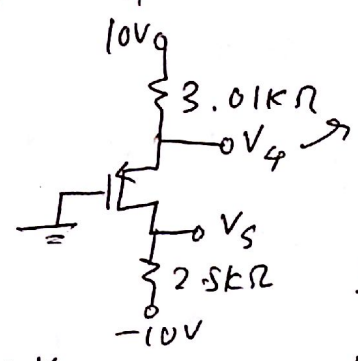
$$V_{GD} = 5V \Rightarrow \text{SAT}^n$$

$$\Rightarrow 2mA = \frac{1m}{2} (V_4 - 2)^2 \rightarrow V_4 - 2 > 0 \rightarrow \text{ON}$$

$$\Rightarrow 4 = (V_4 - 2)^2 \Rightarrow V_4 - 2 = 2 \Rightarrow V_4 = 4V$$

$$|V_{tp}| = 2V$$

$$R = \frac{10 - 4}{2m} = 3k\Omega \Rightarrow$$



we know that $I_D' < I_D$
i.e. drain current decreases
 $V_4 \sim 4V$

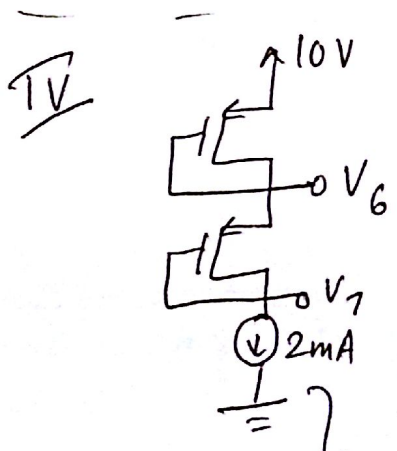
$$\Delta V_S = \Delta I_D \cdot 2.5k$$

$$I_D' = \frac{2 \times 3}{3.01} = 1.9934mA$$

$$V_S = -5 + \Delta V_S$$

$$= -5.0165V //$$

$$\Delta V_S = -0.0165V$$



$$V_D = V_G \text{ both MOSFETs} \Rightarrow \text{SAT}^n$$

$$I_D = 2mA = \frac{1m}{2} (10 - V_6 - 2)^2$$

$$\Rightarrow 4 = (8 - V_6)^2 \Rightarrow 8 - V_6 = 2 \Rightarrow V_6 = 6V$$

$$8 - V_6 > 0 \rightarrow \text{ON}$$

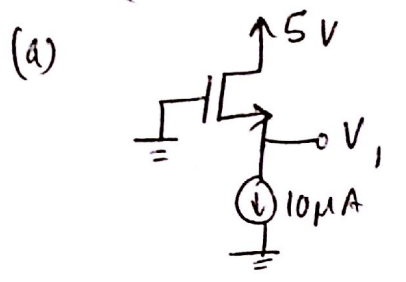
$$I_D = 2mA = \frac{1m}{2} (V_6 - V_7 - 2)^2 \rightarrow 4 - V_6 > 0$$

$$\Rightarrow 2 = 4 - V_7 \Rightarrow V_7 = 2V //$$

$$R = \frac{V_7 - 0}{2m} = 1k\Omega = 1k\Omega \quad (1\% \text{ tolerance value})$$

$$\Rightarrow V_7 = 2V \ \& \ V_6 = 6V !$$

5.56. $k_n'(W/L) = 0.5 \text{ mA/V}^2$, $V_t = 0.8 \text{ V}$, $\lambda = 0$



Assume SATⁿ (✓)

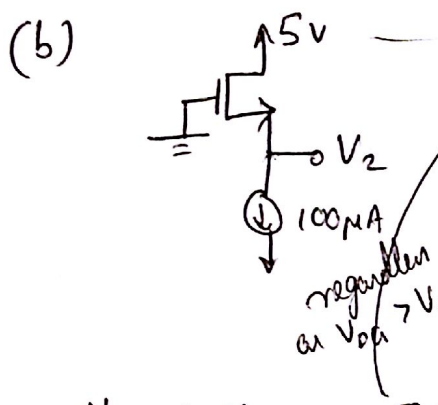
$$I_D = 10 \mu\text{A} = \frac{k_n' W}{2L} V_{ov}^2 = \frac{0.5 \text{ m}}{2} (0 - V_1 - 0.8)^2$$

$\Rightarrow 40 \mu = (V_1 + 0.8)^2 \text{ m}$

$\Rightarrow 40 \text{ m} = (V_1 + 0.8)^2 \Rightarrow (V_1 + 0.8)^2 = 40 \times 10^{-3}$

$\Rightarrow V_1 + 0.8 = \pm(2 \times 10^{-1}) = \pm 0.2$

$\Rightarrow V_1 = -1 \text{ V} \parallel$ $V_{DS} = 5 + 1$, $V_{ov} = 0 + 1 - 0.8$
 $\Rightarrow V_{DS} > V_{ov}$



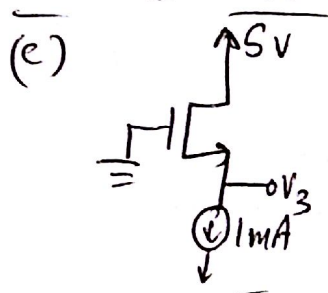
Assume SATⁿ (✓)

$$I_D = 100 \mu\text{A} = \frac{0.5 \text{ m}}{2} (0 - V_2 - 0.8)^2$$

$\frac{200 \mu}{0.5 \text{ m}} = (V_2 + 0.8)^2 \Rightarrow 400 \text{ m} = (V_2 + 0.8)^2$

$\Rightarrow V_2 = -\sqrt{0.4} - 0.8 = -1.43 \text{ V} \parallel$

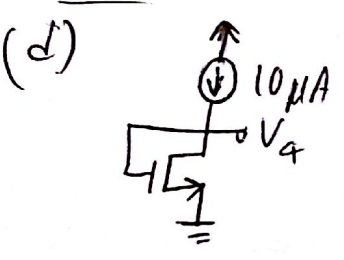
$V_{DS} > V_{ov}$ as $5 - V_2 > 0 - V_2 - 0.8$



$V_{ov} = 5 \text{ V} > -V_t, -0.8 \Rightarrow \text{SAT}^n$

$$I_D = 1 \text{ m} = \frac{0.5 \text{ m}}{2} (-V_3 - 0.8)^2$$

$\Rightarrow 4 = (V_3 + 0.8)^2 \Rightarrow V_3 + 0.8 = -2 \Rightarrow V_3 = -2.8 \text{ V} \parallel$



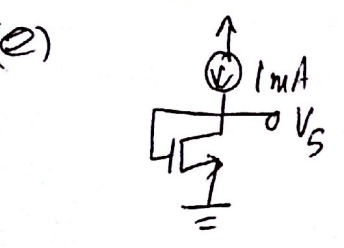
$V_{ov} = 0 > -V_t, -0.8 \Rightarrow \text{SAT}^n$

$$I_D = 10 \mu\text{A} = \frac{0.5 \text{ m}}{2} (V_4 - 0 - 0.8)^2$$

$\Rightarrow \frac{20 \mu}{0.5 \text{ m}} = (V_4 - 0.8)^2 \Rightarrow (V_4 - 0.8)^2 = 40 \text{ m}$

$\Rightarrow V_4 - 0.8 = 2 \times 10^{-1} = 0.2 \Rightarrow V_4 = 1 \text{ V} \parallel$

$V_4 - 0.8 > 0$ (ON)

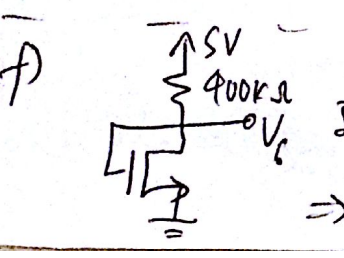


$V_{ov} = 0 > -V_t, -0.8 \Rightarrow \text{SAT}^n$

$$I_D = 1 \text{ mA} = \frac{0.5 \text{ m}}{2} (V_5 - 0 - 0.8)^2$$

$\Rightarrow \frac{2 \text{ m}}{0.5 \text{ m}} = (V_5 - 0.8)^2 \Rightarrow 4 \text{ m} = (V_5 - 0.8)^2$

$\Rightarrow V_5 = 0.8 + \sqrt{4 \times 10^{-3}} = 2.8 \text{ V} \parallel$



$V_{ov} = 0 > -V_t, -0.8 \Rightarrow \text{SAT}^n$

$$I_D = \frac{5 - V_6}{400 \text{ k}} = \frac{0.5 \text{ m}}{2} (V_6 - 0.8)^2$$

$\Rightarrow \frac{1}{20} - \frac{1}{100} V_6 = (V_6 - 0.8)^2 \approx V_6 = 0.8 \text{ V}$ (MAKES SENSE AS I_D is very low)