

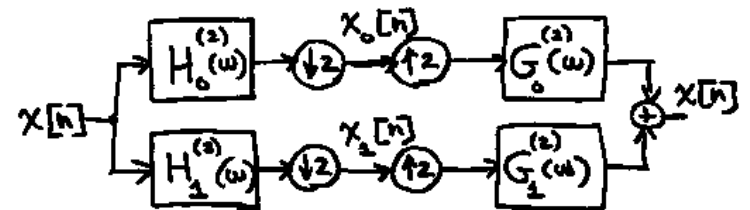
EE648 (CC761-M) DSP II  
 Session 24 (live: 4/8/99)

• Announcement: Session 26 is canceled.

• Outline

- Prelude to DT Wavelets
  - Chap. 11.4 of V. Text

• Recall: 2 channel PR filter bank



• view as an expansion of  $X[n]$  in terms of a set of orthonormal basis functions

• assuming ideal 2-channel QMF

$$X[n] = \sum_{m=0}^1 \sum_{k=-\infty}^{\infty} x_m[k] g_m^{(2)}[n-2k]$$

• wavelet coefficients:

$$x_m[n] = \sum_{k=-\infty}^{\infty} x[k] h_m^{(2)}[2n-k] \quad m=0,1$$

$$x_m[n] \rightarrow \uparrow 2 \xrightarrow{W_m[n]} \boxed{g_m^{(2)}[n]} \rightarrow y_m[n]$$

$$W_m[n] = \sum_{k=-\infty}^{\infty} x_m[k] \delta[n-2k]$$

$$y_m[n] = W_m[n] * g_m^{(2)}[n] = \sum_{k=-\infty}^{\infty} x_m[k] g_m^{(2)}[n-2k]$$

- Orthonormality of wavelet basis:

$$\sum_{n=-\infty}^{\infty} h_m^{(2)}[n-2k] g_l^{(2)*}[n-2i] = \delta[m-l] \delta[k-i]$$

- referred to as bi-orthogonality

- Compare to DFT basis:

- basis fns.:  $g_k[n] = e^{j \frac{2\pi}{N} kn}$ ,  
 $k=0, 1, \dots, N-1$ ,  
 $n=0, 1, \dots, N-1$

- if  $x[n] \neq 0$  only for  $n=0, 1, \dots, N-1$ ,

$$x[n] = \sum_{k=0}^{N-1} \left( \frac{1}{N} X_N(k) \right) g_k[n]$$

- orthonormality of DFT basis:

$$\sum_{n=0}^{N-1} g_k[n] g_l^*[n] = N \delta[k-l]$$

$$\frac{1}{N} X_N(k) = \sum_{n=0}^{N-1} x[n] g_k^*[n]$$